

## Cambridge IGCSE<sup>™</sup>

	CANDIDATE NAME						
	CENTRE NUMBER		CANDIDATE NUMBER				
* 4 7	MATHEMATIC	S	0580/43				
	Paper 4 (Extend	ded)	October/November 2021				
υ 00			2 hours 30 minutes				
	You must answer on the question paper.						
U	You will need:	Geometrical instruments					

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## INSTRUCTIONS

- Answer all questions. •
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs. •
- Write your name, centre number and candidate number in the boxes at the top of the page. •
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid. •
- Do not write on any bar codes. •
- You should use a calculator where appropriate. •
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in • degrees, unless a different level of accuracy is specified in the question.

This document has 20 pages. Any blank pages are indicated.

For  $\pi$ , use either your calculator value or 3.142.

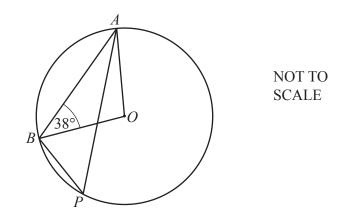
## **INFORMATION**

- The total mark for this paper is 130.
- The number of marks for each question or part question is shown in brackets [].

- 8 7 В 6 5 4 A 3 Т 2 1 0 2 5 x 3 4 Ż 6 Š (a) Describe fully the single transformation that maps triangle T onto triangle A. ......[3] (b) (i) Describe fully the single transformation that maps triangle T onto triangle B. \_\_\_\_\_ (ii) Calculate the distance that each point of triangle T moves when it is mapped onto triangle B.
- 1 The diagram shows three triangles, T, A, and B, drawn on a 1 cm<sup>2</sup> grid.

y

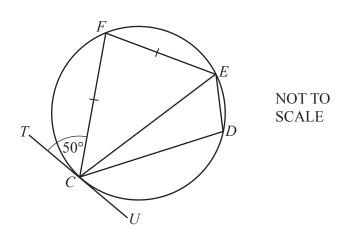
2 (a)



A, B and P are points on a circle, centre O and angle  $OBA = 38^{\circ}$ .

Find angle APB.

**(b)** 



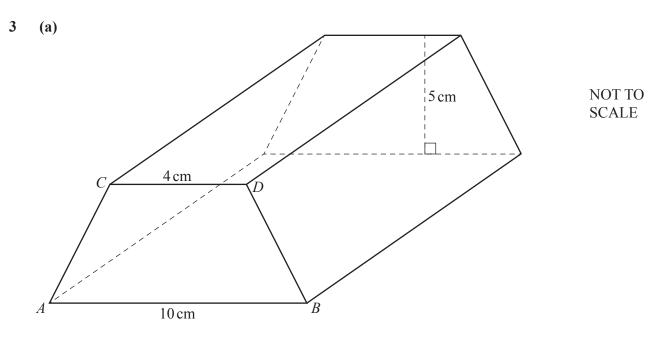
*CDEF* is a cyclic quadrilateral and FC = FE. *TU* is a tangent to the circle at *C* and angle  $TCF = 50^{\circ}$ .

Find

(i) angle *EFC*,

Angle  $EFC = \dots$  [2]

(ii) angle CDE.



The diagram shows a prism. The cross-section of the prism is a trapezium with *CD* parallel to *AB* and AC = BD.

AB = 10 cm, CD = 4 cm and the height of the trapezium is 5 cm. The volume of the prism is 525 cm<sup>3</sup>.

(i) The prism is made of iron.
1 cm<sup>3</sup> of iron has a mass of 7.8 g.

Calculate the mass of the prism. Give your answer in kilograms.

..... kg [2]

(ii) Calculate the length of the prism.

(iii) Calculate the total surface area of the prism.

(iv) In a mathematically similar prism, the height of the trapezium is 10 cm.Calculate the volume of this prism.

..... cm<sup>3</sup> [3]

(b) A cuboid measures 10 cm by 4 cm by 6 cm.Each side is measured correct to the nearest centimetre.

Complete the inequality for the volume, V, of this cuboid.

4 (a) Solve the simultaneous equations. You must show all your working.

$$2p - q = 7$$
$$3p + 2q = 7$$

 $p = \dots$  [3]

(b) Solve the equation.

$$\frac{x}{4} + \frac{2x}{3} = 1$$

(c)  $-8 < 3x - 2 \le 7$ 

(i) Solve the inequality.

......[3]

(ii) Find the integer values of x that satisfy the inequality.

(d) Factorise completely.

$$16a - 4a^2$$

(e) Write each of the following as a single fraction, in its simplest form.

(i) 
$$\frac{1}{2a} \div \frac{3}{4b}$$

......[2]

(ii) 
$$2 - \frac{x}{x-1}$$

.....[2]

5 (a) \$500 is invested at a rate of 3% per year.

Calculate the total interest earned at the end of 7 years when

(i) simple interest is paid,

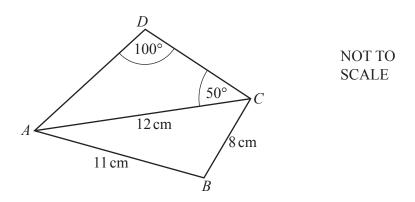
(ii) compound interest is paid.

(b) The value of a car decreases exponentially by 10% each year. The value now is \$6269.40.

Calculate the value of the car 3 years ago.







(a) Calculate *AD*.

(b) Calculate angle BAC and show that it rounds to  $40.42^\circ$ , correct to 2 decimal places.

(c) Calculate the area of the quadrilateral *ABCD*.

..... cm<sup>2</sup> [3]

(d) Calculate the shortest distance from *B* to *AC*.

...... cm [3]

[4]

7 (a) Amir buys 3 cakes that cost c cents each and 2 loaves of bread that cost (2c - 11) cents each. He spends a total of \$5.87.

Find the value of *c*.

(b) A bottle of water costs w. A bottle of juice costs (w + 1).

> Alex spends \$22 on bottles of water and \$42 on bottles of juice. The number of bottles of water is equal to the number of bottles of juice.

Find the value of *w*.

(c) Alicia walks a distance of 9 km at a speed of x km/h. She then runs a distance of 5 km at a speed of (2x + 1) km/h.

The total time Alicia takes is 2.5 hours.

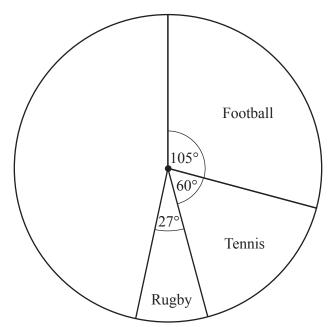
(i) Show that  $10x^2 - 41x - 18 = 0$ .

(ii) Work out Alicia's running speed. You must show all your working.

..... km/h [4]

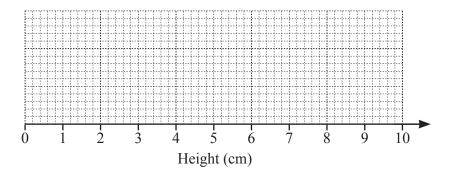
[4]

8 (a) Jean asks 600 people to choose their favourite sport. The pie chart shows some of this information.



- (i) Show that 100 people choose tennis.
- (ii) Work out how many people choose rugby.
- (iii) 125 people choose cricket and the rest choose swimming.Complete the pie chart to show this information.
- (b) The heights of some plants are measured:
  - smallest height =  $0.6 \,\mathrm{cm}$
  - range =  $8.1 \,\mathrm{cm}$
  - median =  $5.2 \,\mathrm{cm}$
  - lower quartile =  $3.4 \,\mathrm{cm}$
  - interquartile range = 4.1 cm.

On the grid, draw a box-and-whisker plot to show this information.



[3]

[1]

[2]

(c) A dice is rolled 100 times. The frequency table shows the results.

Score	1	2	3	4	5	6
Frequency	16	25	17	19	8	15

Find

- (i) the range,
- (ii) the mode,

- ......[1]

(iii) the median.

- (d) 50 students answer a mathematics question. The table shows the time, *t* seconds, taken by each student to answer the question.

Time ( <i>t</i> seconds)	$10 < t \le 20$	$20 < t \le 25$	$25 < t \le 30$	$30 < t \le 50$	$50 < t \le 80$
Frequency	2	8	12	16	12

Calculate an estimate of the mean.

.....s [4]

$$f(x) = x(x-1)(x-2)$$

9

(a) Find the coordinates of the points where the graph of y = f(x) crosses the x-axis.

(.....) (.....) (.....)

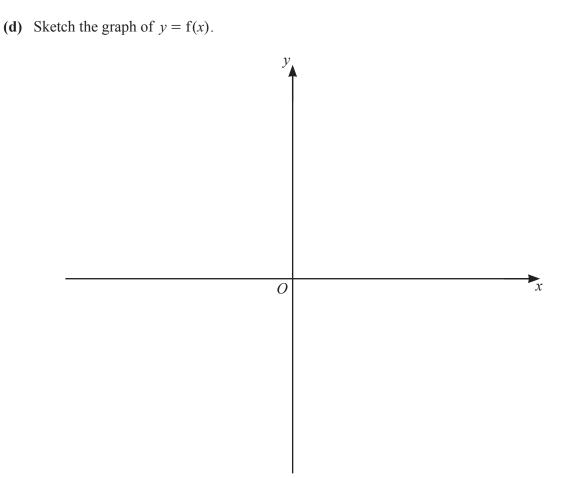
[2]

(b) Show that  $f(x) = x^3 - 3x^2 + 2x$ .

(c) Find the coordinates of the turning points of the graph of y = f(x). Show all your working and give your answers correct to 1 decimal place.

( )	
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(.....) [8]



[2]

- **10** (a) Sarah spins a fair four-sided spinner numbered 0, 1, 1 and 3.
  - (i) What number is the spinner most likely to land on?

......[1]

(ii) Sarah spins the spinner twice.

Find the probability that it lands on the number 1 both times.

......[2]

(iii) Sarah spins the spinner until it lands on the number 3. The probability that this happens on the *n*th spin is  $\frac{729}{16384}$ . Find the value of *n*.

 $n = \dots [2]$ 

(b) Scott takes an examination.

The examination is in two parts, a theory test and a practical test. Both parts must be passed to pass the examination.

The probability that Scott passes the theory test is 0.9. The probability that Scott passes the practical test is 0.8.

Find the probability that

(i) Scott passes the examination,

(ii) Scott passes the theory test or the practical test but not both.

.....[3]

11		f(x)	) = 2x - 1	$g(x) = x^2 + 2x$	$h(x) = 4^x$	$\mathbf{j}(\mathbf{x}) = 2^{\mathbf{x}}$	
	(a)	Fin	d the value of				
		(i)	h(3),				
		(ii)	fh(3).			[	[1]
						[	[1]

(b) Solve the equation gf(x) = 0.

 $x = \dots$  or  $x = \dots$  [4]

(c) 
$$p^{-1}(x) = f(x)$$

Find p(x).

(d) 
$$h(x)j(x) = \frac{1}{\sqrt{2}}$$

Find the value of *x*.

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